

MATH111-002 200630 Sample Midterm Test 1

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October 2, 2006

You have 50 minutes to do each of the following questions. The entire exam is worth 50 marks. You should be able to earn about 1 mark per minute.

1. (10 marks) Find the following derivatives:

- (a) (3 marks) y' where $y = e^{e^x}$
- (b) (3 marks) y' where $y = \log_2(x^3)$
- (c) (4 marks) y' where $y = \sqrt{1 + xe^{-2x}}$

2. (10 marks) Find the following integrals:

- (a) (3 marks) $\int_0^5 e^{-3x} dx$
- (b) (3 marks) $\int \frac{e^x + 1}{e^x} dx$
- (c) (4 marks) $\int x2^{x^2} dx$

3. (10 marks) Let $f(x) = 2x + \cos x$.

- (a) (2 marks) Find $f'(x)$.
- (b) (2 marks) Show that $f'(x) > 0$ for all x .
- (c) (2 marks) Show that f is invertible.
- (d) (2 marks) Find $f^{-1}(1)$.
- (e) (2 marks) Find $(f^{-1})'(1)$.

4. (10 marks) Use logarithmic differentiation to find the following derivatives.

- (a) (3 marks) y' where $y = (2x + 1)^5(x^4 - 3)^6$
- (b) (3 marks) y' where $y = x^{\sin x}$
- (c) (4 marks) y' where $x^y = y^x$.

5. (5 marks) Find $\frac{d^3}{dx^3}(x^2 \ln x)$.

6. (5 marks) Show that $e^x \geq 1 + x$ whenever $x > 0$.